# Longitudinal coupling between electrically driven spin-qubits and a resonator



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### Motivation

- Electron/hole-spin qubits  $\rightarrow$  long coherence times and scalability
- Electric field + Spin orbit interaction  $\rightarrow$  Access spin states [1]
- Floquet qubits more robust against noise than their static counterparts [2]
- Experiment shows that shuttling electron spins enhances their coherence [3]

### System and model Hamiltonian



### Dependence of the coupling on the QD trajectory



Coupling strength as path is varied from a line to a circle. For Ge/SiGe hole-spin  $g_z/2\pi \approx 10$  MHz and  $g_z/2\pi \approx 4$  MHz for GaAs electron spin

### Decoherence

### **Floquet spin-qubit states**

• If  $H_{el}(t+T) = H_{el}(t)$ , with  $T = 2\pi/\Omega$ , solutions to Schrödinger equation  $i\partial_t |\Psi(t)\rangle = H_{el}(t) |\Psi(t)\rangle$  are *Floquet states*  $|\Psi_i(t)\rangle$  written as,

 $|\Psi_{i}(t)\rangle = e^{-i\epsilon_{j}t} |\psi_{i}(t)\rangle, \ j = 0, 1, 2...,$ 

where the *periodic Floquet mode*  $|\psi_i(t)\rangle$  obey:

Following a Floquet-Born-Markov approach, the rate equation for the Floquet spin-qubit in the interaction picture is

$$\dot{\rho}_{S}(t) = \sum_{s=\pm,z} \Gamma_{s} \mathcal{D}_{s}[\rho_{S}(t)],$$

$$\mathcal{D}_{s}[\rho_{S}(t)] = \tau_{s}^{F} \rho_{S}(t)(\tau_{s}^{F})^{\dagger} - \frac{1}{2}\{(\tau_{s}^{F})^{\dagger} \tau_{s}^{F}, \rho_{S}(t)\},$$

$$\Gamma_{\pm} = \left(\frac{\Omega \lambda_{0}}{\omega_{0} \lambda_{SO}}\right)^{2} \sum_{\alpha,k} |m_{\pm,\alpha}(k)|^{2} (k \pm \gamma_{B})^{2} J_{\alpha}[\Omega(k \pm \gamma_{B})]$$

$$z = \left(\frac{\Omega \lambda_{0}}{\omega_{0} \lambda_{SO}}\right)^{2} \sum_{\alpha,k} |m_{z,\alpha}(k)|^{2} k^{2} J_{\alpha}(k\Omega), \ J_{\alpha}(\omega): \text{ bath spectral function}$$

$$\frac{10^{5}}{10^{4}} [(a) \qquad 10^{4} [(b) \qquad 10^{4} ]$$



(a) Relaxation  $1/T_1 = \Gamma_+ + \Gamma_-$  and (b) dephasing  $1/T_2 = \Gamma_z$  rates for hole-based (black, blue, red) and electron-based Floquet spin-qubits (green)

 $(H_{el}(t) - i\partial_t) |\psi_j(t)\rangle = \epsilon_j |\psi_j(t)\rangle, \ |\psi_j(t+T)\rangle = |\psi_j(t)\rangle.$ 

**Qubit states**  $\{|\Psi_{\tilde{q}}^{F}(t)\rangle\}_{\tilde{q}=0,1}$ : Floquet states with most overlap with the lowest two instantaneous ground states of  $H_{el}(t) |\Psi_q^{\text{inst}}(t)\rangle = \epsilon_q^{\text{inst}}(t) |\Psi_q^{\text{inst}}(t)\rangle$ 



Assuming a driven harmonic potential in adiabatic regime with parameters  $E_0 = 0.1$ ,  $\Omega = 0.3$  and  $\omega_0 = 1$ , here we show the plots of  $|\langle \Psi_i^F(t) | \Psi_{1(2)}^{inst}(t) \rangle|^2$ with instantaneous states  $|\Psi_{1(2)}^{inst}(t)\rangle$  and the Floquet states that had the most overlap to choose  $\{|\Psi_i^F(t)\rangle\}_{i=11,12}$  as the qubit states.

## Hamiltonian in the Floquet qubit subspace

 $H_{s-p}(t) = [g_{z}(t)\tau_{z}^{F} + (g_{+}(t)\tau_{+}^{F} + \text{h.c.})](a^{\dagger} + a) + \omega_{c}a^{\dagger}a,$ 

#### • Qubit power dissipation: $P \approx \Gamma_+ \Omega$

### Two qubit CPHASE gate

• For two Floquet spin-qubits, with  $\Delta = \omega_c - \Omega$ , we obtained:  $H_{2q} = \Delta a^{\dagger} a + (g_{z,1}\tau_{z,1}^F + g_{z,1}\tau_{z,2}^F)(a^{\dagger} + a),$ 

known to realise a CPHASE gate [5] for a gate time  $t_g = \pi \Delta / (8g_{z,1}g_{z,2})$ . For Ge/SiGe hole-spin  $t_q \approx 50$  ns and for GaAs electron spin  $t_q \approx 100$  ns, show that  $t_q \ll T_1 \sim 0.1$  ms

### Geometric origin of the interaction

• For general  $U(\mathbf{r})$ , the geometric nature of the interaction is revealed in instantaneous frame defined by the unitary  $\mathcal{U} \equiv \mathcal{U}[\mathbf{E}(t)]$ ,

 $H_{s-p} = E_{c,\beta} \dot{E}_{\alpha} \left( m_{\alpha\beta}^{z} \tau_{z}^{F} + m_{\alpha\beta}^{+} e^{i\epsilon_{q}t} \tau_{+}^{F} + \text{h.c.} \right) (a^{\dagger} + a),$ 

where  $m_{\alpha\beta}^{z}(t), m_{\alpha\beta}^{+}(t) \propto \mathcal{F}_{\alpha\beta}^{E}$  where,  $\mathcal{F}_{\alpha\beta}^{E} = \partial_{\alpha}\mathcal{A}_{\beta}^{E} - \partial_{\beta}\mathcal{A}_{\alpha}^{E} + i[\mathcal{A}_{\alpha}^{E}, \mathcal{A}_{\beta}^{E}]$  is the Berry curvature and  $\mathcal{A}^{E}_{\alpha} = i\mathcal{U}^{\dagger}\partial_{E_{\alpha}}\mathcal{U}$  is the Berry connection

$$g_{z}(t) = \frac{R_{c}}{2} \cdot \frac{d}{dt} \left[ \langle \psi_{1}(t) | \boldsymbol{m} | \psi_{1}(t) \rangle - \langle \psi_{0}(t) | \boldsymbol{m} | \psi_{0}(t) \rangle \right],$$
  
$$g_{+}(t) = i e^{i\epsilon_{q} t} R_{c} \cdot \left( \epsilon_{q} - i \frac{d}{dt} \right) \langle \psi_{1}(t) | \boldsymbol{m} | \psi_{0}(t) \rangle, \ \boldsymbol{m} = \begin{bmatrix} \sigma_{x} & -\sigma_{y} \end{bmatrix}^{T}$$

Longitudinal term  $g_z(t) \rightarrow 0$  in static case

### Longitudinal readout

The readout of the Floquet spin-qubit can be achieved faster [4] by utilizing longitudinal spin-photon couplings instead of transverse interactions due to better pointer separation at initial times as,

$$a(t)\rangle = -i\left(g_z(k=1)/\kappa\right)\langle\tau_z^F\rangle(1-e^{-\kappa t/2})$$

### **Conclusion & Outlook**

- Defined Floquet spin-qubit, unraveled tunable transverse and longitudinal spin-photon coupling to a resonator, constructed a CPHASE two-qubit gate, and estimated the coherence in the presence of ohmic noise
- Revealed the geometric nature of interaction using adiabatic perturbation theory
- Future: Generalise to multiple qubits and evaluate the phonon-induced decoherence

#### References

[1] Golovach et al., PRA **81**, 022315 (2010) [2] Huang et al., PRA **15**, 034065 (2021) [3] Mortemousque et al., PRXQ **2**, 030331 (2021) [4] Didier et al., PRL **115**, 20360 (2015) [5] Harvey et al., PRB **97**, 235409 (2018)



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