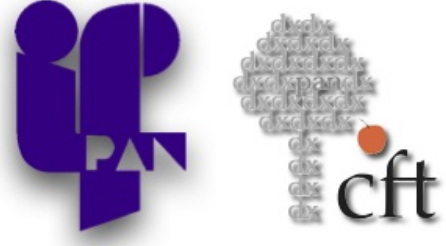


Spontaneous breaking of the time-reversal symmetry in optical lattices

Tomasz Sowinski



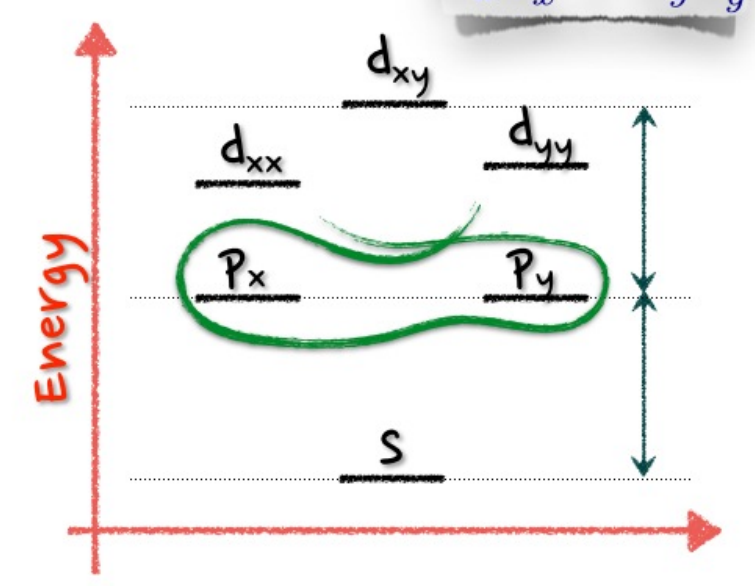
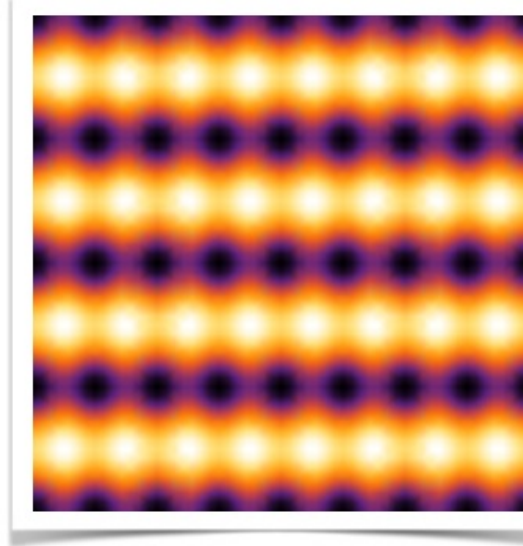
1D optical chain (with p-band degeneracy)

$$V(x, y) = V_x \sin^2(k_x x) + V_y \sin^2(k_y y)$$

in non-symmetric rectangular optical lattice it is possible to obtain the degeneracy between single-particle orbitals in p-band by a proper adjustment of the lattice parameters

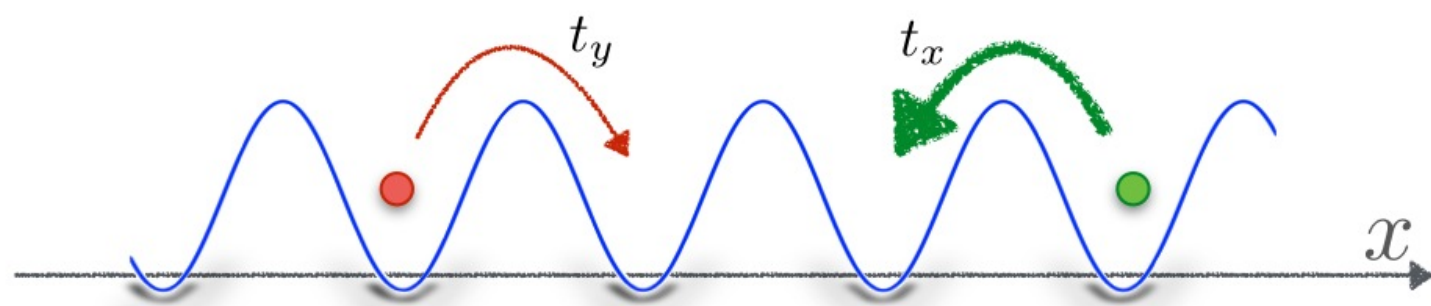
in harmonic approximation

$$V_x k_x^2 = V_y k_y^2$$



single-particle tunnelings

$$\hat{H} = \sum_i \hat{H}(i) - \sum_{\langle ij \rangle} [t_x \hat{a}_x^\dagger(i) \hat{a}_x(j) + t_y \hat{a}_y^\dagger(i) \hat{a}_y(j) + h.c.]$$



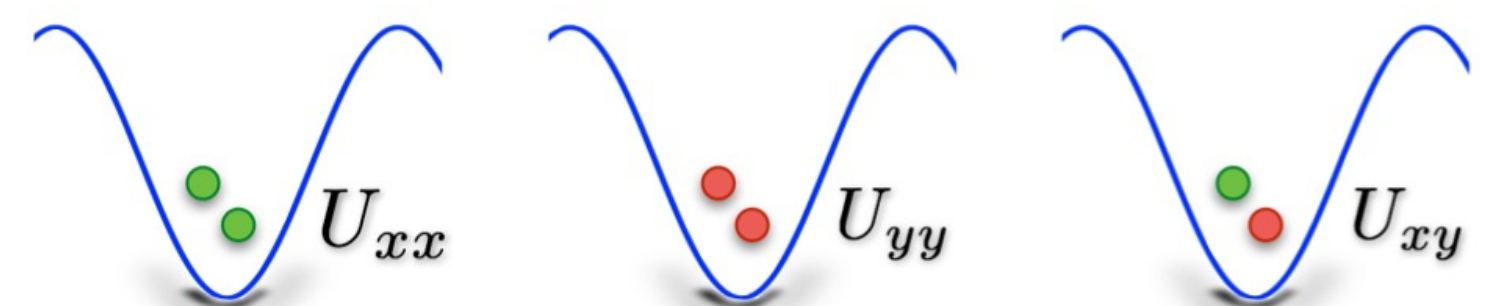
$$|t_x| > |t_y|$$

- - p_x boson
- - p_y boson

two-particle interactions

$$\hat{H}(i) = \frac{U_{xx}}{2} \hat{n}_x(i)(\hat{n}_x(i) - 1) + \frac{U_{yy}}{2} \hat{n}_y(i)(\hat{n}_y(i) - 1) + \frac{U_{xy}}{2} [4\hat{n}_x(i)\hat{n}_y(i) + \hat{a}_x^\dagger(i)^2 \hat{a}_y(i)^2 + \hat{a}_y^\dagger(i)^2 \hat{a}_x(i)^2]$$

local Hamiltonian



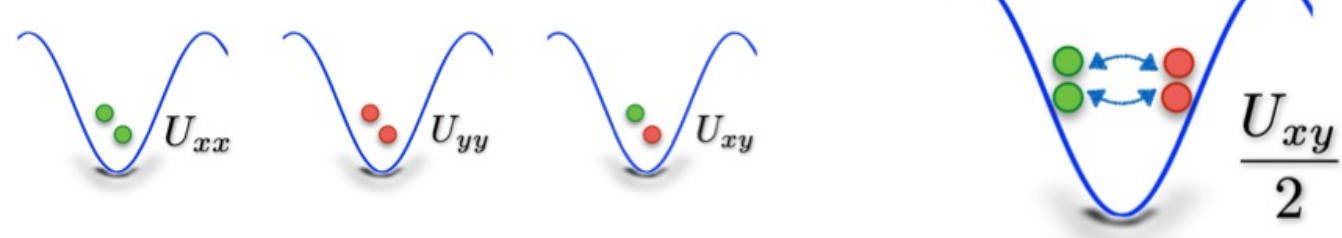
- - p_x boson
- - p_y boson

degeneracy is lifted by anharmonicity
 $U_{yy} > U_{xx} > 3U_{xy}$

p-orbital physics

$$\hat{H} = \sum_i \hat{H}(i) - \sum_{\langle ij \rangle} [t_x \hat{a}_x^\dagger(i) \hat{a}_x(j) + t_y \hat{a}_y^\dagger(i) \hat{a}_y(j) + h.c.]$$

local Hamiltonian



total number of particles is conserved

$$[\hat{H}, \hat{N}_x + \hat{N}_y] = 0$$

additional symmetry of the system

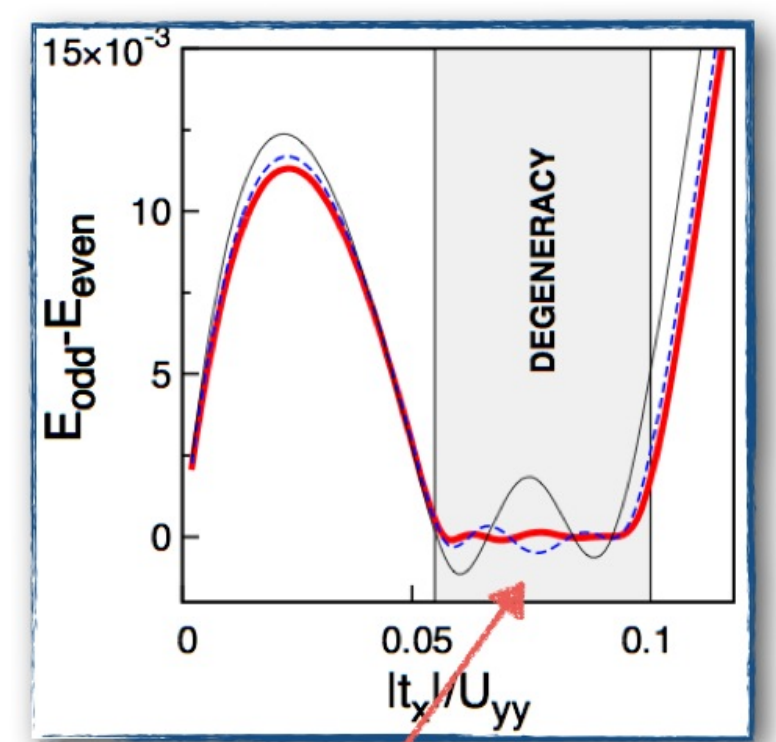
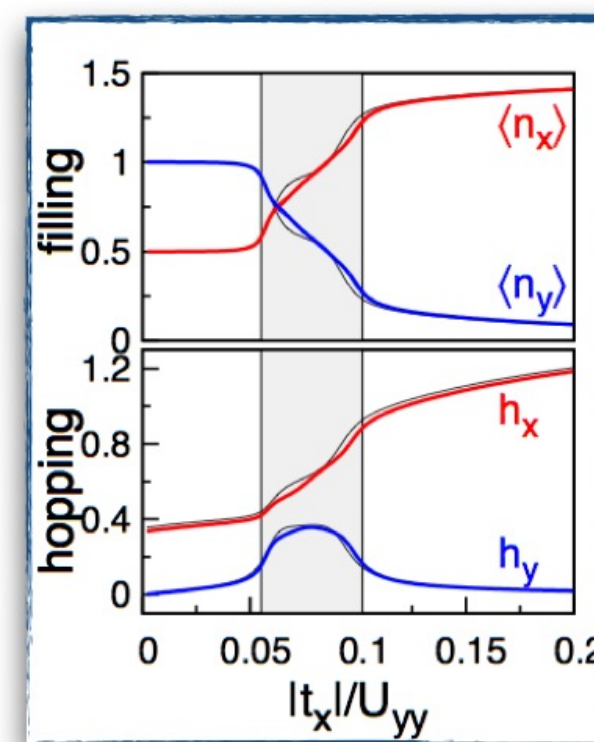
$$\hat{S} = \exp(i\pi \hat{N}_y)$$

$$\hat{N}_x = \sum_i \hat{n}_x(i)$$

$$\hat{N}_y = \sum_i \hat{n}_y(i)$$

p-orbital physics

3/2 filling



$$h_x = \langle G | \hat{a}_x^\dagger(i) \hat{a}_x^\dagger(i+1) | G \rangle$$

$$h_y = \langle G | \hat{a}_y^\dagger(i) \hat{a}_y^\dagger(i+1) | G \rangle$$

two-fold degeneracy of the many-body ground state
 $|G_{\text{odd}}\rangle$ $|G_{\text{even}}\rangle$

region of restored degeneracy

two-fold degeneracy of the many-body ground state

$$|G\rangle = \cos\theta |G_{\text{odd}}\rangle + \sin\theta e^{i\varphi} |G_{\text{even}}\rangle$$

many-body ground state in the thermodynamic limit

Chosen ground state should be as close to the product state as possible

Einselction principle
W. H. Zurek, Rev. Mod. Phys. 75, 715 (2003)

entanglement entropy for single lattice site

$$S(\theta, \varphi) = -\sum_i \lambda_i \log \lambda_i$$

eigenvalues of the single-site reduced density matrix

$$|G_{\pm}\rangle = \frac{|G_{\text{odd}}\rangle \pm i |G_{\text{even}}\rangle}{\sqrt{2}}$$

properties of the ground-state

$$|G_{\pm}\rangle = \frac{|G_{\text{odd}}\rangle \pm i |G_{\text{even}}\rangle}{\sqrt{2}}$$

non-trivial correlations

$$C_{\alpha\beta}(j) = \langle \hat{a}_\alpha^\dagger(j) \hat{a}_\beta(j) \rangle \neq 0$$

$$C_{\alpha\beta}(j) = -C_{\beta\alpha}(j)$$

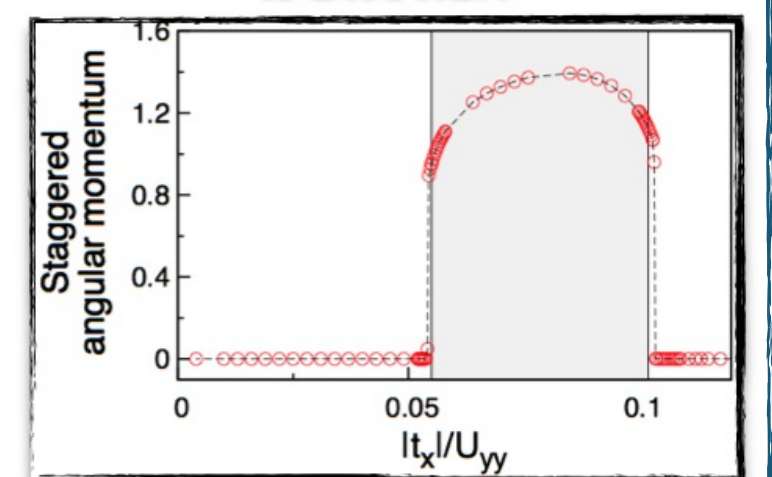
local quasi-angular momentum operator

$$\hat{L}_z(j) = i [\hat{a}_x^\dagger(j) \hat{a}_y(j) - \hat{a}_y^\dagger(j) \hat{a}_x(j)]$$

staggered angular momentum operator

$$\hat{L}_z = \sum_j (-1)^j \hat{L}_z(j)$$

time-reversal symmetry is BROKEN



conclusions

in asymmetric lattices it is possible to obtain degeneracy between the single-particle energies in given orbital (p-orbital)

this degeneracy is lifted by an anharmonicity when contact interactions are taken into account

BUT

the degeneracy between orbitals is dynamically restored due to tunneling

In this region an additional symmetry of the system is spontaneously broken

The state which breaks the time-reversal symmetry becomes the true ground state of the system

references

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Tunneling-Induced Restoration of the Degeneracy and the Time-Reversal Symmetry Breaking in Optical Lattices

Tomasz Sowinski,^{1,2,3} Mateusz Łącki,⁴ Omjyoti Dutta,^{2,4} Joanna Pietraszewicz,¹ Piotr Sierant,⁴ Mariusz Gajda,^{1,3} Jakub Zakrzewski,^{4,5} and Maciej Lewenstein^{2,6}

¹Institute of Physics of the Polish Academy of Sciences, Aleja Lotników 32/46, PL-02-668 Warsaw, Poland
²ICFO, The Institute of Photonic Sciences, Avenue Carl Friedrich Gauss, No. 3, E-08860 Castelldefels (Barcelona), Spain
³Center for Theoretical Physics of the Polish Academy of Sciences, Aleja Lotników 32/46, PL-02-668 Warsaw, Poland
⁴Instytut Fizyki imienia Mariana Smoluchowskiego, Uniwersytet Jagielloński, Ulica Reymonta 4, PL-30-059 Kraków, Poland
⁵Mark Kac Complex Systems Research Center, Uniwersytet Jagielloński, Ulica Reymonta 23, E-08010 Barcelona, Poland
⁶ICREA, Institució Catalana de Recerca i Estudis Avançats, Lluís Companys 23, E-08010 Barcelona, Spain
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We study the ground-state properties of bosons loaded into the *p* band of a one-dimensional optical lattice. We show that the phase diagram of the system is substantially affected by the anharmonicity of the lattice potential. In particular, for a certain range of tunneling strength, the full many-body ground state of the system becomes degenerate. In this region, an additional symmetry of the system, namely, the parity of the occupation number of the chosen orbital, is spontaneously broken. The state with a nonvanishing staggered angular momentum, which breaks the time-reversal symmetry, becomes the true ground state of the system.