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## USEFUL RELATIONSHIPS FOR ROTATIONAL SPECTROSCOPY

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CODATA 2006:  $I_b(\text{u}\text{\AA}^2) = 505\,379.005(36)/B(\text{MHz})$ , 1 rad = 57.295 78° = 180/π  
 where  $505\,379.01 = 10^{20}h/(8\pi^2m_u10^6)$  1 cal = 4.184 J  
 $k/hc = 0.695\,035\,6\text{ cm}^{-1}\text{ K}^{-1}$  1 D = 3.335 641 × 10<sup>-30</sup> C m  
1 Pa = 7.500 617 mTorr

1 bohr = 1  $a_0 = 4\pi\epsilon_0\hbar^2/(m_e e^2) = 0.529\,177\,2\text{ \AA}$   
 1 hartree = 1  $E_h = 27.211\,395\text{ eV} = 2\,625.500\,7\text{ kJ mol}^{-1}$  1 kJ mol<sup>-1</sup> = 83.593 5 cm<sup>-1</sup>  
= 2 506.07 GHz  
 au of dipole = 2.541 746 D

au of quadrupole = 1.345 034 D $\text{\AA}$  (D $\text{\AA}$  = Buckingham = 10<sup>-20</sup> esu)

au of octopole = 0.711 761 4 × 10<sup>-34</sup> esu

au of polarizability = 0.148 184 7  $\text{\AA}^3$

$\chi_{\alpha\alpha}$  (MHz) = -234.964 7  $Q(\text{barn}) \frac{\partial^2 V}{\partial \alpha^2}(\text{au})$  Q(barn) = 0.002860(15) [D], 0.02044(3) [<sup>14</sup>N]  
-0.08165(80) [<sup>35</sup>Cl]  
0.313(3) [<sup>79</sup>Br], -0.710(10) [<sup>127</sup>I]

tetrahedral angle:  $\alpha = \cos^{-1}(-1/3) = 109.471\,22^\circ$

for an XCH<sub>3</sub>-type molecule:  $\sin \beta = \frac{2}{\sqrt{3}} \sin \frac{\alpha}{2}$ , where:  $\angle \text{XCH} = 180 - \beta$ ,  $\angle \text{HCH} = \alpha$

Cartesian → Polar:

Polar → Cartesian:

$R = (x^2 + y^2 + z^2)^{1/2}$

$\theta = \cos^{-1}(z/R)$

$\varphi = \tan^{-1}(y/x)$  [use ATAN2 for quadrant]

$x = R \sin \theta \cos \varphi$

$y = R \sin \theta \sin \varphi$

$z = R \cos \theta$

Least-squares fit of a straight line  $y = a + bx$ :

$C_{xx} = \sum x^2 - (\sum x)^2/N$

$b = C_{xy}/C_{xx}$

$C_{yy} = \sum y^2 - (\sum y)^2/N$

$(\delta b)^2 = \frac{1}{(N-2)C_{xx}}(C_{yy} - bC_{xy})$

$C_{xy} = \sum xy - \sum x \sum y/N$

$a = \frac{1}{N}(\sum y - b \sum x)$

$(\delta a)^2 = \delta b^2 \sum x^2/N$

Error propagation:

$x = aA \pm bB$ :

$\delta x = (a^2\delta A^2 + b^2\delta B^2)^{1/2}$

$x = AB$ :

$\delta x = (A^2\delta B^2 + B^2\delta A^2)^{1/2}$

$x = A/B$ :

$\delta x = [(x/A)^2\delta A^2 + (x/B)^2\delta B^2]^{1/2} = (\delta A^2 + x^2\delta B^2)^{1/2}/B$

$x = 1/A$ :

$\delta x = \delta A/A^2$

$x = A^2$ :

$\delta x = 2A \delta A$

$x = \sqrt{A}$ :

$\delta x = \delta A/(2\sqrt{A})$

$x = \ln A$ :

$\delta x = \delta A/A$

$x = (A^2 + B^2)^{1/2}$ :

$\delta x = (A^2\delta A^2 + B^2\delta B^2)^{1/2}/x$

$x = f(A, B, \dots)$ :

$\delta x^2 = \left(\frac{\partial f}{\partial A}\right)^2 \delta A^2 + \left(\frac{\partial f}{\partial B}\right)^2 \delta B^2 + \dots$